

Modèles hiérarchiques (et réduction de modèles)

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– CNRS UMR 7633 –*

- *Macroscopic models*
- *Uniform fields approaches*
- *Microstructure computations*
- *Examples*

Centre des Matériaux



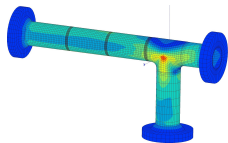
Idea
League



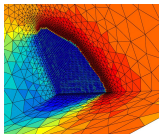
<http://mat.ensmp.fr>



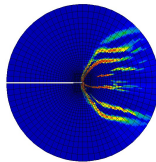
CoCaS: Mechanics of materials and structures



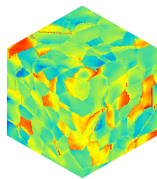
*Structural
computations*



*Crack propagation
with cohesive
zone models*



*Portevin-
Le Chatelier
effect*



*Microstructure
calculations*

- *Georges Cailletaud*
- *Samuel Forest*
- *David Ryckelynck*

20 PhD students, 3 post-doc

Modèles de calcul

- *Les modèles de conception de structure (modèles, codes)*
Ces modèles (règles de construction) doivent être simples de manipulation et stocker sous forme éventuellement heuristique les connaissances sur des conceptions analogues. Pour ces modèles, la robustesse prime sur la performance.
- *Les modèles d'analyse de structure (modèles phénoménologiques)*
Ce sont des modèles, éventuellement raffinés, destinés à l'étude de problèmes de champ sur un objet dont la géométrie, les matériaux, les conditions aux limites et les chargements sont connus. Pour ces modèles, la performance et la robustesse doivent faire l'objet d'un compromis équilibré.
- *Les modèles de compréhension du comportement de la matière (modèles multi-échelles)*
Leur objectif principal est la compréhension fine du comportement à l'échelle locale. Pour ces modèles, la performance prime complètement sur la robustesse.

Stratégie de développement

- *Développement d'un code de calcul "maison"* Le développement du solveur Eléments finis *Zébulon* a commencé en 1982; le code *Z-set* qui en est issu est maintenant codéveloppé par le CDM, l'ONERA/DMSE, NorthWest Numerics, avec des coopérations à l'UTT et à l'ENS Cachan
- *Une librairie de modèles de matériaux* Une attention toute particulière est mise dans la représentation des comportements non-linéaires des matériaux; la librairie *Z-mat* est interfacée avec les principaux codes commerciaux
- *Les langages "orientés-objet"* Le choix du C++ est fait en 1992, avec réécriture totale du code
- *Le parallélisme* Utilisation d'un solveur parallèle (FETI) valide sur machine à mémoire *distribuée*, en coopération avec l'ONERA

Les buts du calcul de microstructures

- *Comprendre le "fonctionnement" du matériau* Etre capable de reproduire par la simulation un comportement est un gage de compréhension des mécanismes élémentaires
- *Obtenir des champs locaux, entrée des modèles de rupture* Le phénomène de rupture étant local, il est naturel qu'il soit modélisé à l'aide de variables de l'échelle locales, contraintes et déformations à l'échelle des grains dans un alliage, à l'échelle des phases dans un composite, par exemple
- *Créer une véritable "ingénierie des matériaux"* Etre capable de prévoir des propriétés mécaniques ou physiques sans produire le matériau; optimiser le matériau vis-à-vis d'une sollicitation donnée

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 - Homogenization problems
 - Characterisation of local stress/strain fields
 - Stress corrosion cracking in Zircaloy
 - Fretting–wear tests
 - Modeling of fully controlled microstructures

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Ingredients of a mechanical model (small strain)

- *Strain partition*

$$\underline{\underline{\epsilon}} = \underline{\underline{\epsilon}}^e + \underline{\underline{\epsilon}}^{in} = \underline{\underline{\epsilon}}^e + \underline{\underline{\epsilon}}^p + \underline{\underline{\epsilon}}^{vp}$$

with

$$\underline{\underline{\sigma}} = \underline{\underline{\Lambda}} : \underline{\underline{\epsilon}}^e$$

- *Flow rules*

- *Plasticity*

$$\dot{\underline{\underline{\epsilon}}}^p = \dot{\lambda} \underline{\underline{n}} \quad \dot{\lambda} \text{ from } \dot{f} = 0$$

- *Viscoplasticity*

$$\dot{\underline{\underline{\epsilon}}}^{vp} = \dot{p} \underline{\underline{n}} \quad \dot{p} = \left\langle \frac{f}{K} \right\rangle^n$$

- *Hardening rules*

$$\dot{Y}_I = \text{fct}(Y_I, \underline{\underline{\epsilon}}^p, \underline{\underline{\epsilon}}^{vp})$$

Common formalism for plasticity and viscoplasticity

- **Same equations** for the strain partition and hardening rules
- Only the flow rule will differ: see for instance a model with von Mises criterion and isotropic hardening,

$$f(\underline{\sigma}) = J(\underline{\sigma}) - R(p) - \sigma_y$$

- **Plasticity** (point expected to be on the yield surface at the end of the increment)

$$f = 0 \quad J(\underline{\sigma}) - R(p) - \sigma_y = 0$$

- **Viscoplasticity** (point expected to be on the relevant equipotential at the end of the increment)

$$f > 0 \quad J(\underline{\sigma}) - R(p) - \sigma_y + K\dot{p}^{1/n} = 0$$

$$\text{or } J(\underline{\sigma}) - R(p) - \sigma_y + K \left(\frac{\Delta p}{\Delta t} \right)^{1/n} = 0$$

Common formalism for small and large strain

- **Same equations** for the flow and hardening rules
- Only the partition rule will differ:

- *Small strain*

$$\tilde{\boldsymbol{\varepsilon}} = \tilde{\boldsymbol{\varepsilon}}^e + \tilde{\boldsymbol{\varepsilon}}^{in}$$

- *Large strain*

$$\tilde{\mathbf{F}} = \tilde{\mathbf{E}}\tilde{\mathbf{P}}$$

Case of multipotential models

- Strain partition, **unchanged**

$$\underline{\underline{\epsilon}} = \underline{\underline{\epsilon}}^e + \underline{\underline{\epsilon}}^{in} = \underline{\underline{\epsilon}}^e + \underline{\underline{\epsilon}}^p + \underline{\underline{\epsilon}}^{vp}$$

- Elasticity, **unchanged**

$$\underline{\underline{\sigma}} = \underline{\underline{\Lambda}} : \underline{\underline{\epsilon}}^e$$

- Flow rules

- Plasticity (e.g. crystal plasticity)

$$\dot{\underline{\underline{\epsilon}}}^p = \sum_s \dot{\lambda}^s \underline{\underline{m}}^s \quad \dot{\lambda}^s \text{ from } \dot{f}^s = 0$$

$$\text{for active systems} \quad f^s = |\tau^s| - \tau_c = 0$$

- Viscoplasticity

$$\dot{\underline{\underline{\epsilon}}}^{vp} = \sum_s \dot{v}^s \underline{\underline{m}}^s \quad \dot{v}^s = \left\langle \frac{f^s}{K} \right\rangle^n$$

- Hardening rules

$$\dot{Y}_I = fct(Y_I, \underline{\underline{\epsilon}}^p, \underline{\underline{\epsilon}}^{vp})$$

Flow under strain rate control

$$\dot{\underline{\underline{\sigma}}} = \underline{\underline{\Lambda}} : (\dot{\underline{\underline{\epsilon}}} - \dot{\underline{\underline{\epsilon}}^P}) \quad \text{and} : \quad \underline{\underline{n}} : \dot{\underline{\underline{\sigma}}} = H\dot{p}$$

$$\dot{\lambda} = \dot{p} = \frac{\underline{\underline{n}} : \underline{\underline{\Lambda}} : \dot{\underline{\underline{\epsilon}}}}{H + \underline{\underline{n}} : \underline{\underline{\Lambda}} : \underline{\underline{n}}}$$

$$\dot{\underline{\underline{\sigma}}} = \underline{\underline{\Lambda}} : (\dot{\underline{\underline{\epsilon}}} - \dot{\underline{\underline{\epsilon}}^P}) = \left(\underline{\underline{\Lambda}} - \frac{(\underline{\underline{\Lambda}} : \underline{\underline{n}}) \otimes (\underline{\underline{n}} : \underline{\underline{\Lambda}})}{H + \underline{\underline{n}} : \underline{\underline{\Lambda}} : \underline{\underline{n}}} \right) : \dot{\underline{\underline{\epsilon}}}$$

Continuous tangent operator $\underline{\underline{L}}_t$

Note: for isotropic elasticity and von Mises material,

$$\dot{\lambda} = \frac{2\mu \underline{\underline{n}} : \dot{\underline{\underline{\epsilon}}}}{H + 3\mu}$$

Anatomy of constitutive equations

- *Definitions:*
 - External parameters (ep) *imposed as input*
 - Integrated variables ($vint$)
 - Auxiliary variables ($vaux$), *just for output*
 - Coefficients ($coef$), *material parameters*
 - Primal and dual variables, *prescribed variables and associated fluxes*
- *Three sets of equations are to be considered*
 - *Strain partition (1 tensorial variable)*
 - *Plastic/viscoplastic flow (1 scalar variable for each potential)*
 - *Hardening rules (model dependent)*

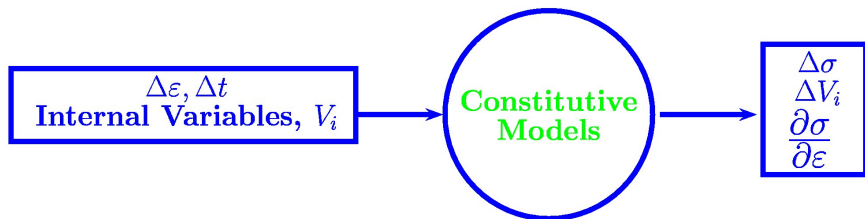
Primal and dual variables in various fields

problem	primal	dual
<i>mechanics, small perturbation</i>	$\underline{\underline{\epsilon}}$	$\underline{\underline{\sigma}}$
<i>mechanics, large deformation</i>	$\underline{\underline{\mathbf{F}}}$	$\underline{\underline{\mathbf{\Pi}}}$
<i>thermal pb</i>	$(T, \underline{\underline{\text{grad} T}})$	$(H, \underline{\underline{\mathbf{q}}})$
<i>diffusion</i>	concentration	flux
<i>electrostatics</i>	$\underline{\underline{\text{grad} V}}$	$\underline{\underline{\mathbf{E}}}$
<i>magnetostatics</i>	rot $\underline{\underline{\mathbf{A}}}$	$\underline{\underline{\mathbf{H}}}$

$\underline{\underline{\epsilon}}$ strain tensor, $\underline{\underline{\mathbf{F}}}$ deformation gradient, T temperature, V electric potential, $\underline{\underline{\mathbf{A}}}$ potential vector, $\underline{\underline{\sigma}}$ Cauchy stress tensor, $\underline{\underline{\mathbf{S}}}$ second Piola–Kirchhoff stress tensor, H enthalpy, $\underline{\underline{\mathbf{q}}}$ thermal flux, $\underline{\underline{\mathbf{E}}}$ electric field, $\underline{\underline{\mathbf{H}}}$ magnetic field.

Generic interface for any constitutive equation

For each Gauss Point...

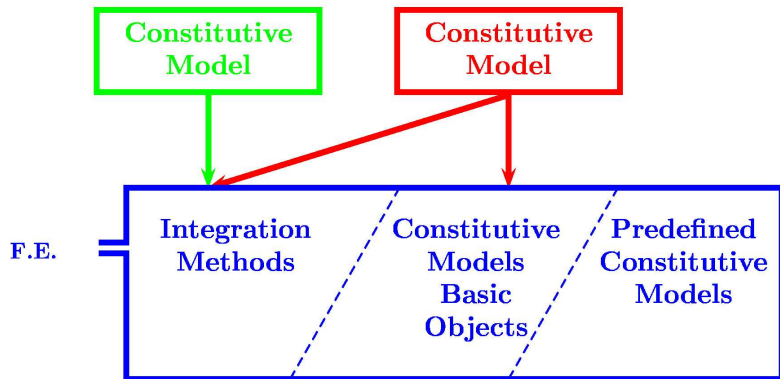


Example of the material library *Z-mat*

- *Numerous material models, plus user material*
- *Interface with the classical FE softwares*
- *Provide automatic time stepping and consistent tangent stiffness*
- *Coefficients presenting unlimited dependence on internal variables*
- *ZeBFRoNT, automatic code generation*
- *MuLTiMaT concept, for recursive multiscale modeling*

[zval@mat.ensmp.fr]

What is inside *Z-mat* ?

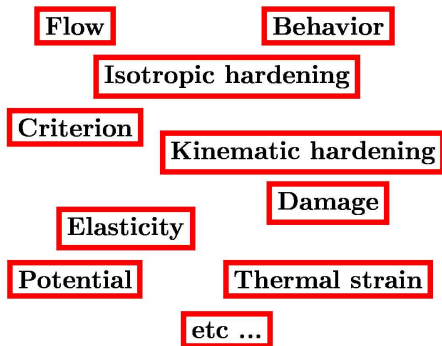


- Runge-Kutta
- Theta method

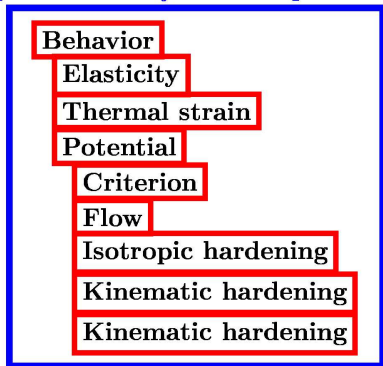
- Elasticity
- Thermal Strain
- Isotropic Hardening
- Kinematic Hardening
- ...

Object oriented modular design in *Z-mat*

Material objects



Typical assembly for viscoplasticity



Isotropic and nonlinear kinematic model in Z -mat

behavior

elasticity isotropic

thermal strain isotropic

potential ev

criterion mises

flow norton

isotropic nonlinear

kinematic nonlinear

$$\underline{\underline{\epsilon}}^{th} = \alpha(T - T_{ref})$$

$$f = J (\underline{\underline{\sigma}}' - \sum_i \underline{\underline{X}}_i) - R$$

$$\dot{p} = \left\langle \frac{f}{K} \right\rangle^n, \quad \underline{\underline{\dot{\epsilon}}}^{ev} = \dot{p} \underline{\underline{n}}$$

$$R = R_0 + Q(1 - e^{-bp})$$

$$\underline{\underline{X}} = \frac{2}{3} C \underline{\underline{\alpha}}, \quad \underline{\underline{\dot{\alpha}}} = \dot{p} \left[\underline{\underline{n}} - \frac{3D}{2C} \underline{\underline{X}} \right]$$

Example of data files in *Z-mat*

Plasticity

```
***behavior gen_evp
**elasticity isotropic
  young 100000.
  poisson 0.3
**potential gen_evp ep
*criterion mises
*flow plasticity
*isotropic nonlinear
  R0 210. Q 50. b 10.
*kinematic nonlinear
  C 20000. D 500.
```

Viscoplasticity

```
***behavior gen_evp
**elasticity isotropic
  young 100000.
  poisson 0.3
**potential gen_evp ev
*criterion mises
*flow norton
  K 1000. n 4.5
*isotropic nonlinear
  R0 210. Q 50. b 10.
*kinematic nonlinear
  C 20000. D 500.
```

Crystal viscoplasticity

```
***behavior gen_evp
**elasticity cubic
  y1111 100000.
  y1122 75000.
  y1212 112000.
**potential octahedral
*flow norton
  K 1000. n 4.5
*isotropic nonlinear
  R0 210. Q 50. b 10.
*kinematic nonlinear
  C 20000. D 500.
*interaction slip
h1 1. h2 1.2 h3 1.4 h5 1.3 h6 1.
```

ZeBFRoNT concept

- *Preprocessor, using building bricks like elasticity, flow, etc...*
- *Use a macrolanguage, with a limited number of keywords like Coefs, StrainPart, derivative, implicit, etc...*
- *Generate C++ code*

Explicit programming with *ZeBFRoNT*

```
@Class NORTON_BEHAVIOR : BASIC_NL_BEHAVIOR
{
  @Name norton;
  @SubClass ELASTICITY elasticity;
  @Coefs K, n;
  @tVarInt eel;
  @sVarInt evcum;
};
@StrainPart {
  sig = *elasticity*eel;
  m_tg_matrix=*elasticity;
}
@Derivative {
  TENSOR2 sprime,norm;
  double J;
  sig=*elasticity*eel;
  sprime=deviator(sig);
  J=sqrt(1.5*(sprime|sprime));
  devcum=pow(J/K, n);
  norm=sprime*(1.5/J);
  deel=deto-devcum*norm;
}
```

Nom du comportement

Objet matrice d'élasticité

Coefficients de Norton

Variable interne tensorielle : $\underline{\underline{\varepsilon}}_e$

Variable interne scalaire : p

Calcul de la contrainte après intégration

$$\underline{\underline{\sigma}} = \underline{\underline{E}} \underline{\underline{\varepsilon}}_e$$

Matrice tangente approchée (RK !)

Calcul du vecteur dérivé $\underline{\underline{Y}}$

Calcul du déviateur $\underline{\underline{\sigma}}'$

Calcul du deuxième invariant

Fluage de Norton : $\dot{p} = \left(\frac{J}{K}\right)^n$

Direction de l'écoulement

Déformation élastique

Implicit programming with ZeBFRoNT

```
@CalcGradF {
  ELASTICITY& E=*elasticity;
  sig = E*eel;
  f_vec_eel -= deto;
  TENSOR2 sigeff = deviator(sig);
  double J = sqrt(1.5*(sigeff|sigeff));
  if (J>(double)0.0) {
    TENSOR2 norm = sigeff*(1.5/J);
    f_vec_eel += norm*devcum;
    f_vec_evcum -= dt*pow(J/K,n);
    SMATRIX dn_ds = unit32;
    dn_ds -= norm ^ norm;
    dn_ds *= theta*devcum/J;

    deel_deel += dn_ds *E;

    deel_devcum += norm;
    double dv_df = tdt*n*pow(J/K,n-1)/K;
    TENSOR2 df_fs = dv_df*norm;
    devcum_deel -= df_fs*E;
  }
}
```

Intégration implicite

$$\underline{\underline{\sigma}} = \underline{\underline{E}} \underline{\underline{\varepsilon}}$$

$$\underline{\underline{R}}_e = \Delta \underline{\underline{\varepsilon}}_e - \Delta \underline{\underline{\xi}}$$

Déviateur $\underline{\underline{\sigma}}'$

Deuxième invariant

Si on a plastifié

Direction de l'écoulement $\underline{\underline{n}}$

$$\underline{\underline{R}}_e = \Delta \underline{\underline{\varepsilon}}_e - \Delta \underline{\underline{\xi}} + \Delta p \underline{\underline{n}}$$

$$\Delta p = \left(\frac{J}{K}\right)^n \Delta t$$

$$\frac{\partial \underline{\underline{R}}_e}{\partial \Delta \underline{\underline{\varepsilon}}_e}$$

$$\frac{\partial \underline{\underline{R}}_e}{\partial \Delta p}$$

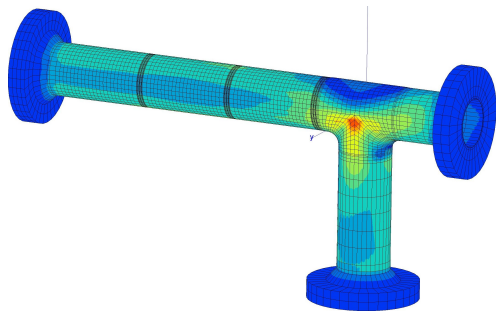
$$\frac{\partial R_p}{\partial \Delta \underline{\underline{\varepsilon}}_e}$$

$$\frac{\partial R_p}{\partial \Delta p} = 1$$

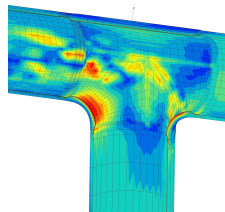
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Tubes in nuclear power plants



Contour of the von Mises stress



Zoom on the critical area

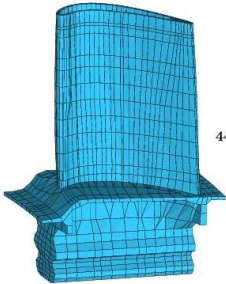
600 000 dof's, 1000 time steps

Collaboration with EDF

Turbine blades (SNECMA)



1992
première simulation
3500 degrés de liberté



1997
aube entière
44000 degrés de liberté

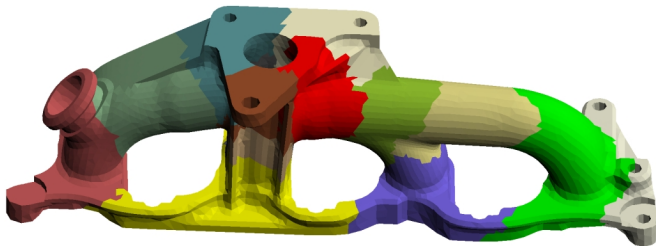


2000
560000 degrés de liberté

Parallel computation, cycle skip

1992: One slice only 1997: Real 3D computation with viscoplastic constitutive equations 2000: Mesh taking into account the detailed geometry

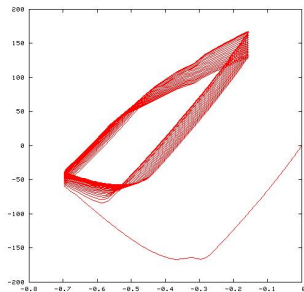
Exhaustion system in car engine (Renault)



345000 dof's, viscoplastic computation including aging
Subdomains in a mesh for parallel computation

GEN-EVP - Application to Aluminum with aging

If aging is purely time based, direct integration can be used and the effect applied to all material coefficients



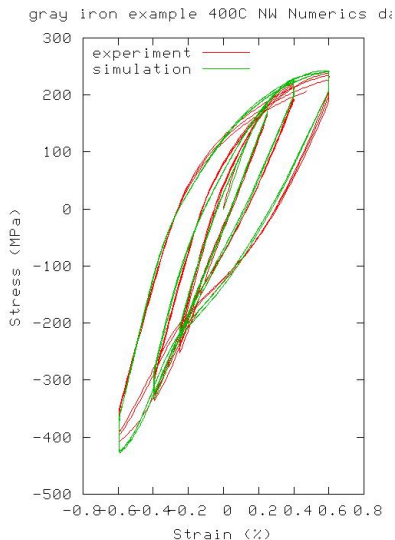
```
%the **auxiliary aging option is part of the base behavior,  
%and can therefore be used to implement time based (or  
%weakly coupled) coefficient dependencies  
%
```

```
**auxiliary aging age_1  
aging_inf temperature  
0. 0.  
0.5 200.  
0.7 280.  
0.9 324.  
  
tau temperature  
1.e+07 0.  
1.e+06 150.  
1.e+05 200.  
12500. 250.  
2500. 280.  
500. 300.  
100. 324.
```

```
*kinematic nonlinear X1  
C aging_effects param:age_1 factor:1.0 temperature  
16000. 0.  
15000. 20.  
0. 324.  
D 100.
```

Cast Iron material Model

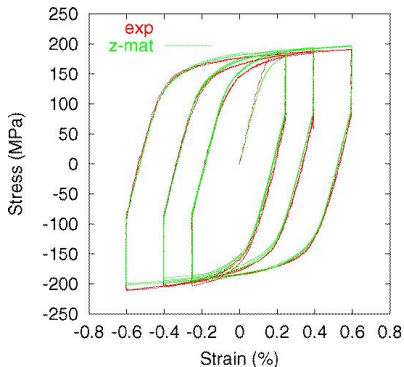
- **Very general framework including :**
 - *Viscoplasticity and flow rule*
 - *Nonlinear kinematic hardening with no limit on number of terms*
 - *Isotropic hardening / softening*
 - *Adjustable damage evolution strain closure shifts compressive with damage, opening occurs at zero stress*
 - *Fatigue damage terms correlated to peak stress and accumulated plasticity*
- **Successfully used in production FEA (e.g. ABAQUS) for more than 5 years now**



GEN-EVP - SiMo type Materials

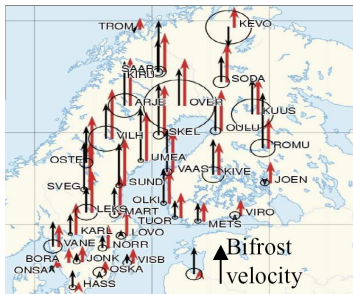
- **Viscoplasticity**

- *Rate law should take into account wide range of rates ... Norton summation or multiple deformation potentials*
- *Kinematic hardening is necessary even if yield radius is zero! Kinematic shift of yield locus*
- *Static recovery required for full relaxation at very high temperatures*
- *Relatively high number of temperatures required to calibrate e.g. 23, 150, 225, 300, 375, 450, 525, 600, 720, 740, 800...*

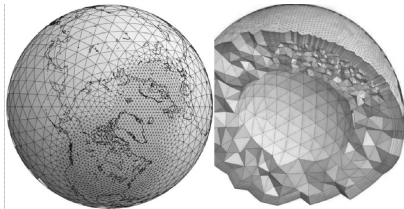


For structures like exhaust manifolds, the viscous effects are important to determine transient effects..e.g. frictional movements and structural ratchetting rates

Post-glacial rebound

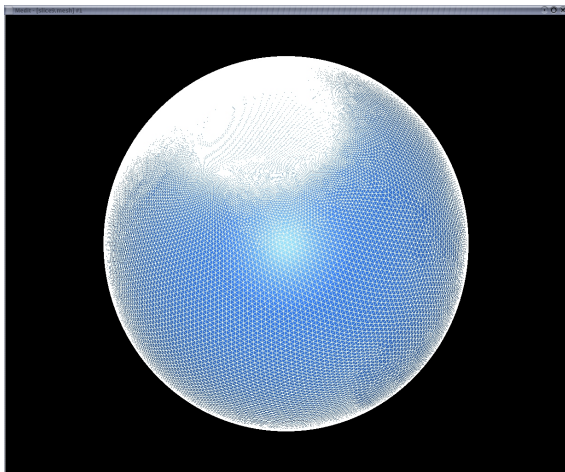


- 20000 years ago, a big amount of ice on Scandinavia and Canada (until 3000 m)
- Ice melting, the continents go up
- Question 1: Sea level ?
- Question 2: Earth mantle viscosity (earthquake prediction)



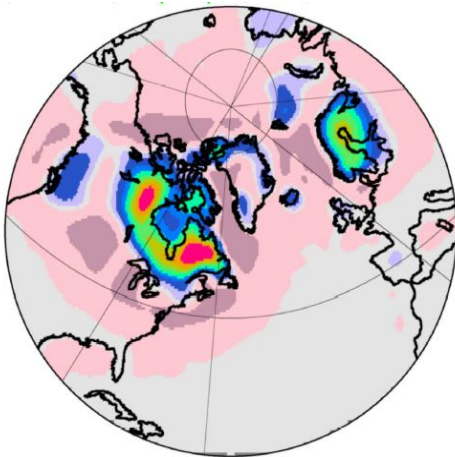
Collaboration with ENS Ulm

Post-glacial rebound: *New meshes*



9600000 dof's, 100 processors

Post-glacial rebound: *First results*



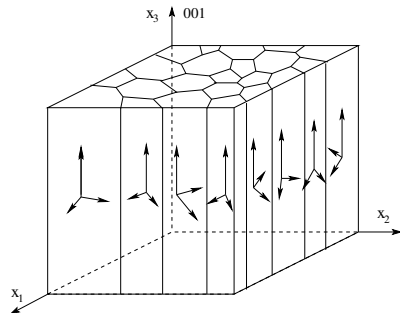
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The limits of the classical yield criteria

- *Initial texture, texture evolution*
 - *Directionnally solidified materials*
 - *Metal forming*
- *Need for a local information in phases*
 - *Phase transformation, several coexisting phases*

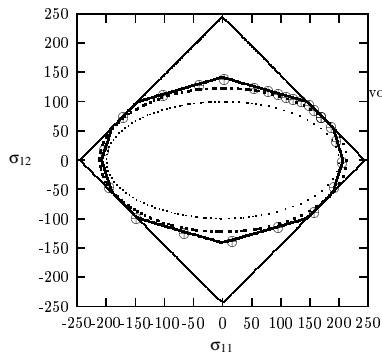
Loading surface of a directionally solidified material (DS)



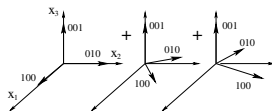
- For a DS material, all the grains have a common crystal axis, say (001). The orientation of each grain is then defined by one angle around this axis.
- Assuming that elasticity is uniform, the stress is also uniform during the elastic phase.

[Sai et al., 2006]

Yield surface for DS material with *3 orientations*



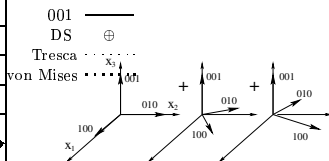
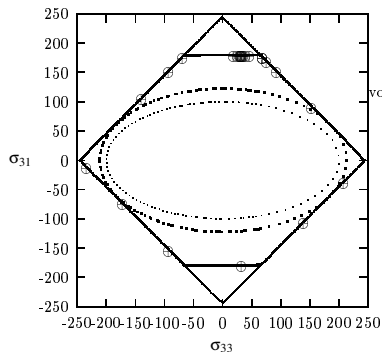
001 ———
DS ⊕
Tresca ·····
von Mises - · - ·



- Orientations of the grains: 0, 30, 60 degrees

More slip directions in the plane σ_{11} - σ_{12} : the model turns out to become similar to von Mises/Tresca

Yield surface for DS material with *3 orientations*

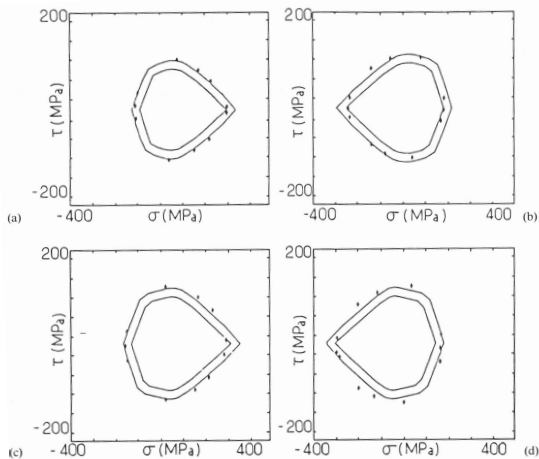


- *Orientations of the grains: 0, 30, 60 degrees*
- *Try an other set*
[HERE](#)

No additional slip activated by shear in the plane σ_{33} - σ_{13} : the yield stress in shear remains high, and sharp corners are still present

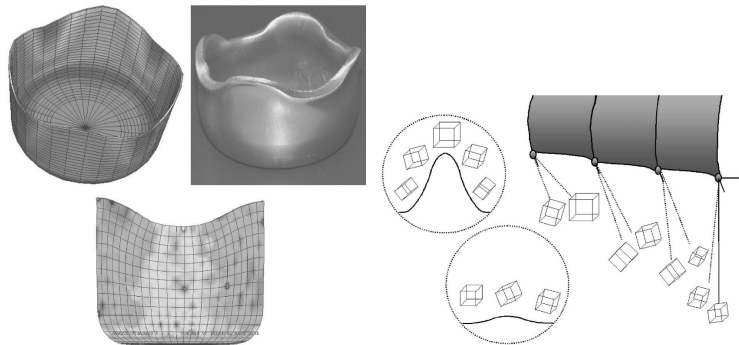
Simulation of the distortion of a yield surface

First cycle and second cycles, 2024 aluminium alloy



[Cailletaud, 1992]

Deep drawing, one polycrystal for each Gauss point



([Raabe and Roters, 2004])

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What comes out microstructure computations

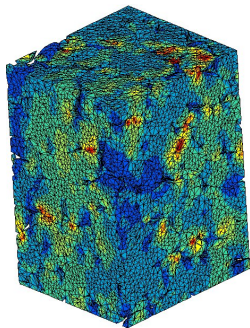
- *Homogenization results*
 - *Equivalent properties for a given microstructure*
- *Results in each phase*
 - *Average values in each phase*
- *Intragranular fields, results near grain boundaries*
 - *Local values inside grains*
- *Real fields in critical zones*
 - *when microstructure size is not small wrt stress gradients*

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Two-phase refractory materials

- Aim: predict the thermomechanical behaviour



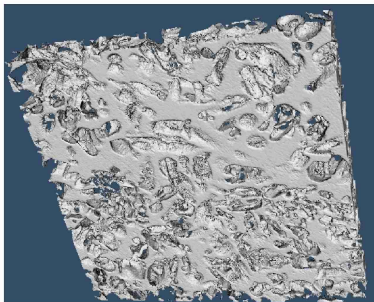
Calculation on a RVE
 $350\mu\text{m} \times 350\mu\text{m} \times 350\mu\text{m}$



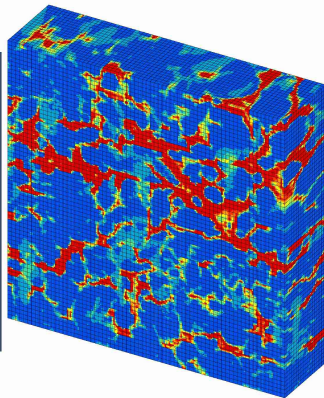
1300 000 node mesh
 $350\mu\text{m} \times 350\mu\text{m} \times 700\mu\text{m}$

[Madi et al., 2007]

Ice cream



imagerie 3D confocale



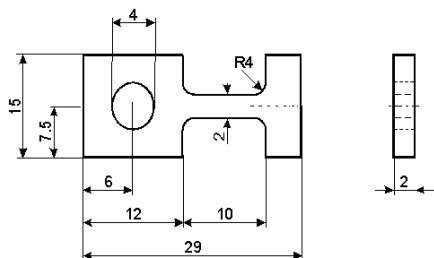
calcul parallèle à 10^6 ddi

[Kanit et al., 2003]

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A test on small OFHC copper specimens



Tension tests on a small flat specimen made of OFHC copper

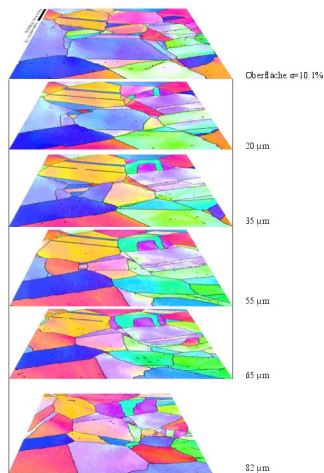
Data available:

- *Macro stress-strain curve*
- *SEM images*
- *OIM scans*
- *Local strain field*

[Tatschl and Kolednik, 2003, Tatschl and Kolednik, 2004]

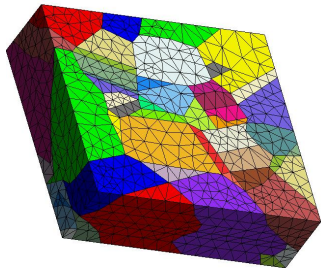
Erich Schmid Institute of Material Science, Leoben, Austria

3D grain morphology information

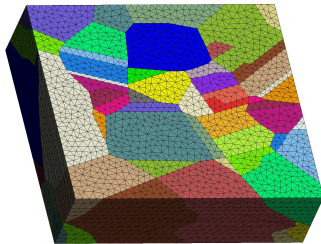


- *After the test, 6 layers of material were successively removed*
- *Final depth – 100 µm*
- *OIM-analysis was made after each removal*
- *3D grain structure can be reconstructed*

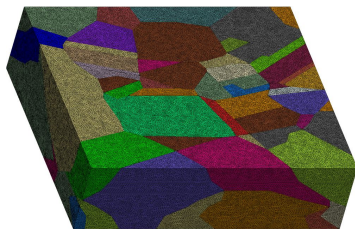
Polycrystal computations



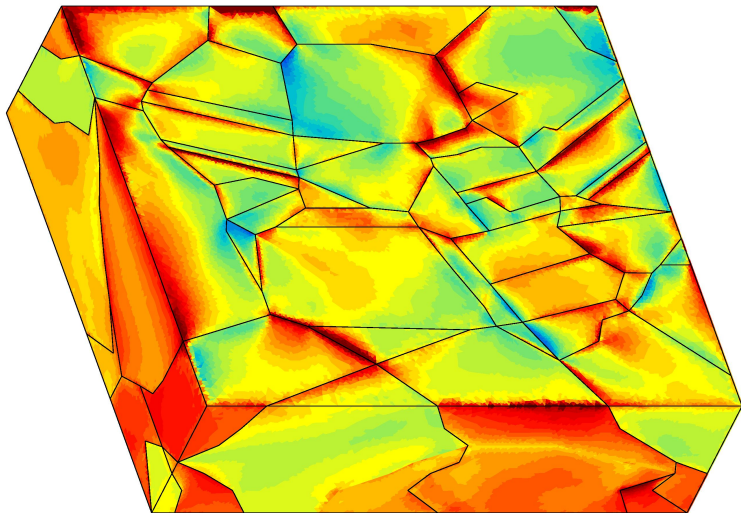
30 000 nodes



130 000 nodes



Local strain in a polycrystal

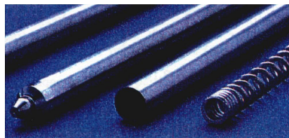


[Musienko et al., 2007]

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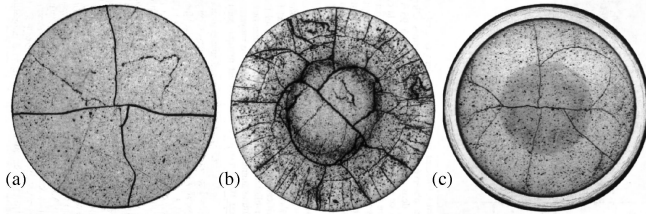
Presentation of the industrial framework



- *Integrity of fuel assemblies of PWR*
- *Fuel rods made of uranium dioxide pellets piled in a Zr4 cladding*
- *Zr4 cladding is the first protection to avoid fission products spreading*
- *Incident called Pellet – Cladding Interaction*

[Diard, 2001, Musienko, 2005]

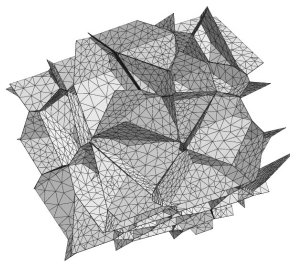
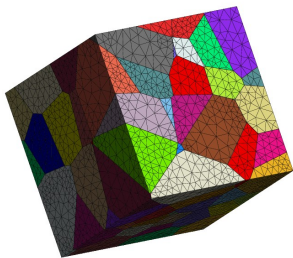
Pellet Crack Patterns



After one irradiation cycle

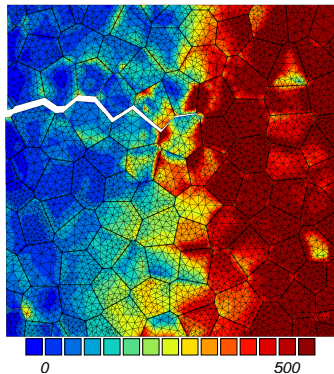
- *Expansion of the uranium oxide, then indentation of the tube by the fragments*
- *Dimension of the tube : diameter 8 mm, thickness 0.7 mm*

3D - a 100 grain aggregate

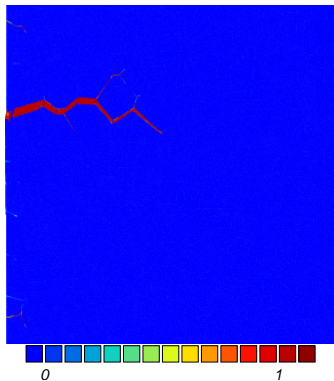


- *2 element boundaries, hexahedra, prisms, tetrahedra, quadratic and quadratic/linear elements*
- *Local orientation to determine normal to the grain boundary*

2D iodine-influenced intergranular fracture (DOS+iodine)

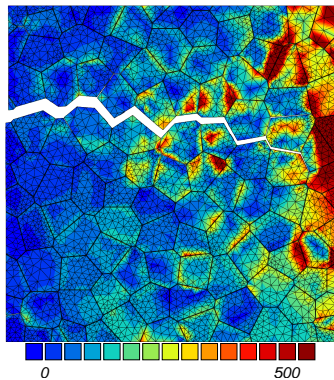


mises stress

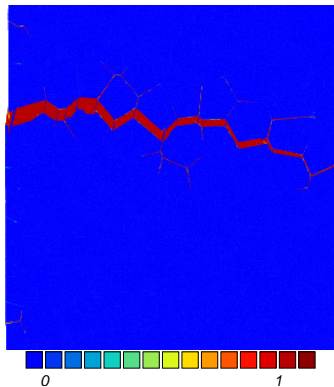


damage

2D iodine-influenced intergranular fracture (DOS+iodine)

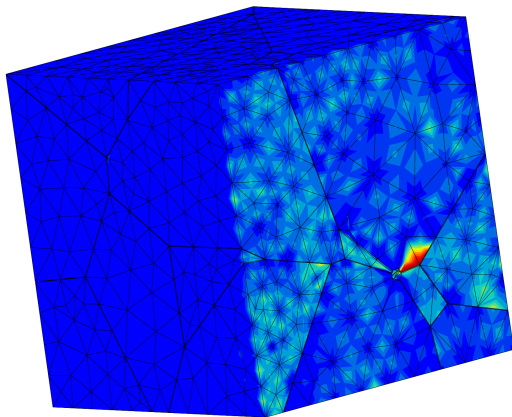


mises stress



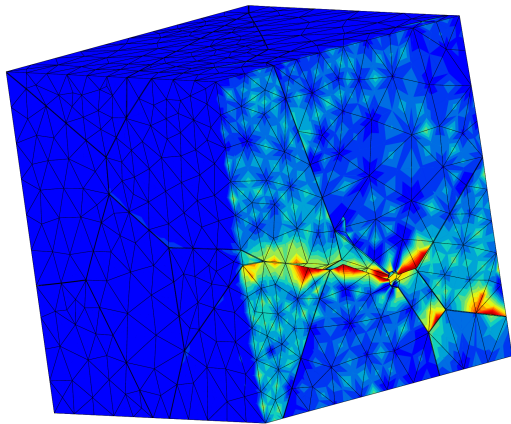
damage

Crack opening



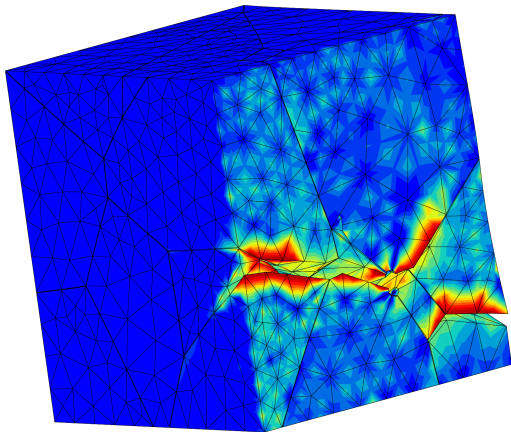
[Cailletaud et al., 2004]

Crack opening



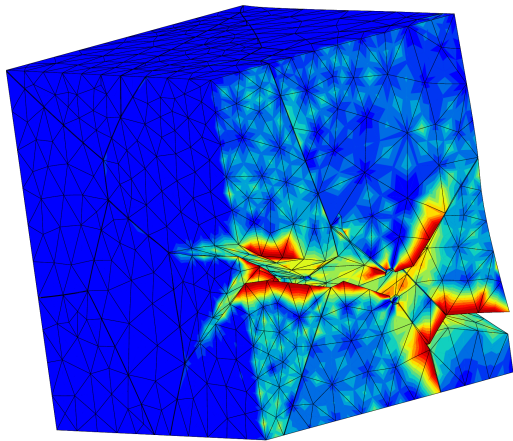
[Cailletaud et al., 2004]

Crack opening



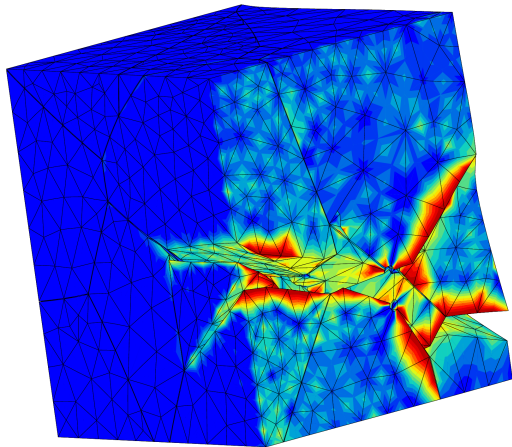
[Cailletaud et al., 2004]

Crack opening



[Cailletaud et al., 2004]

Crack opening

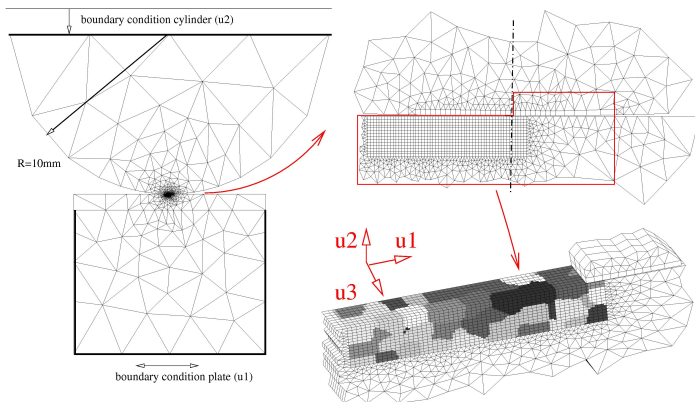


[Cailletaud et al., 2004]

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3D FE model of a fretting wear test

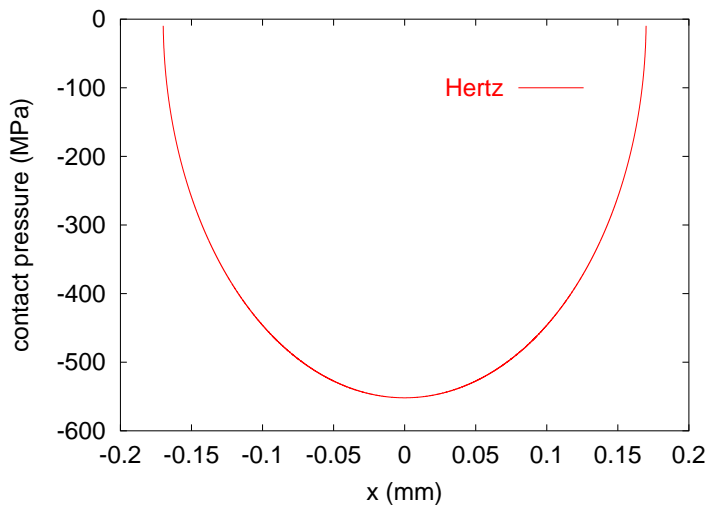


Computation settings

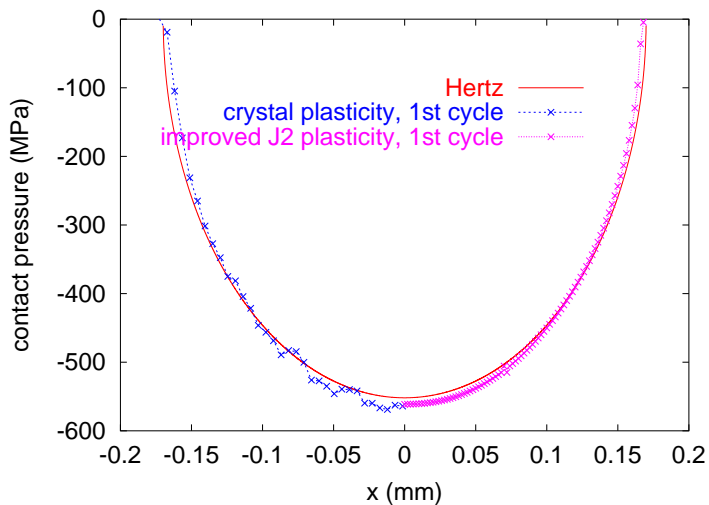
mesh	<i>linear plane strain elements</i>
u3	<i>zero displacement on front and back planes</i>
u2	<i>set to cause vertical force $P = 133\text{ N}$</i>
u1	$\delta_{\max} = 75\ \mu\text{m}$
friction coefficient	<i>0.8</i>
cycling frequency	<i>5 Hz</i>

- *element size in contact $5.4\ \mu\text{m} \times 5.4\ \mu\text{m} \times 6.3\ \mu\text{m}$*
- *small deformations formulation*

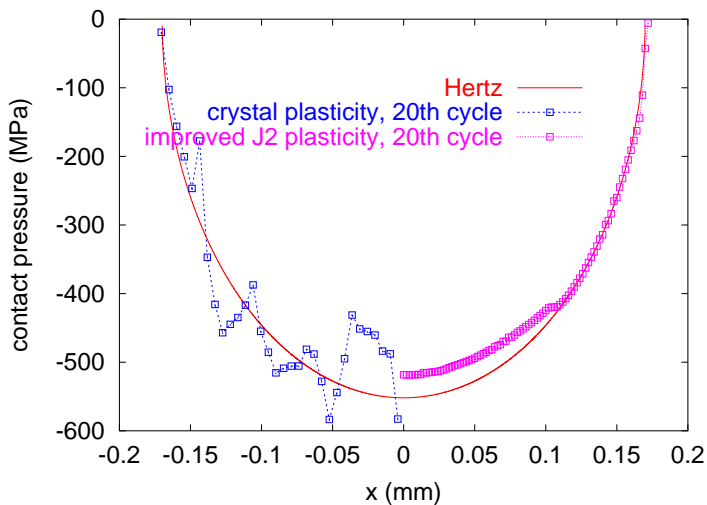
Computation Results: contact pressure



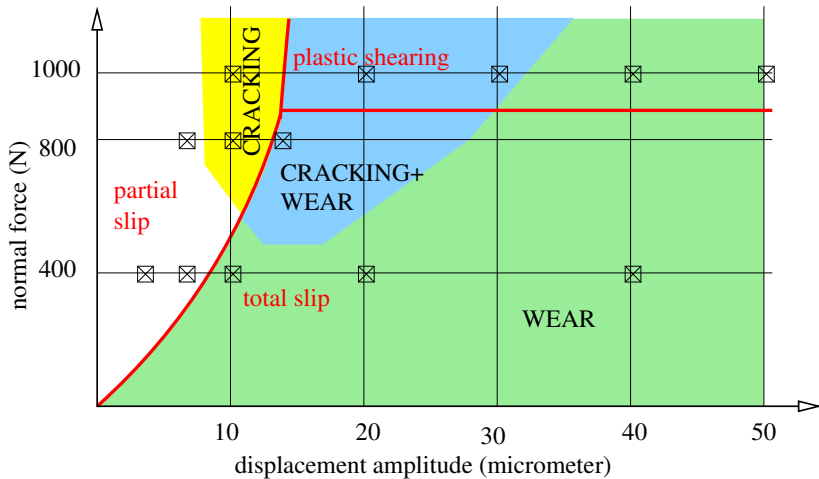
Computation Results: contact pressure



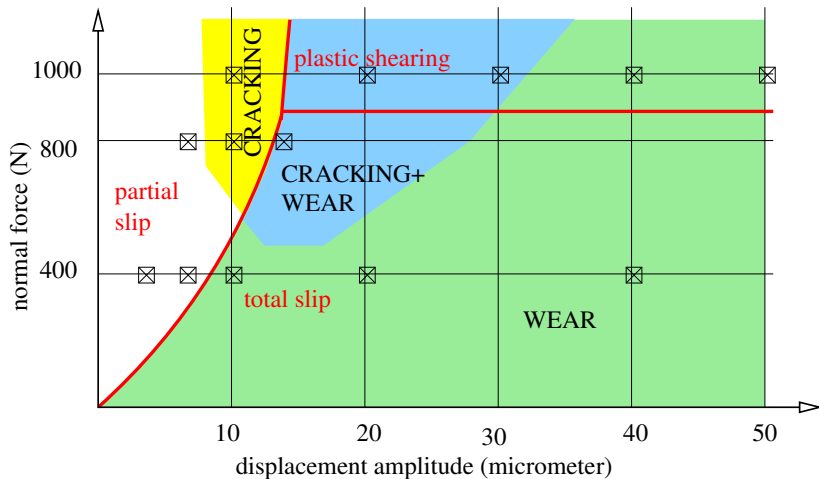
Computation Results: contact pressure



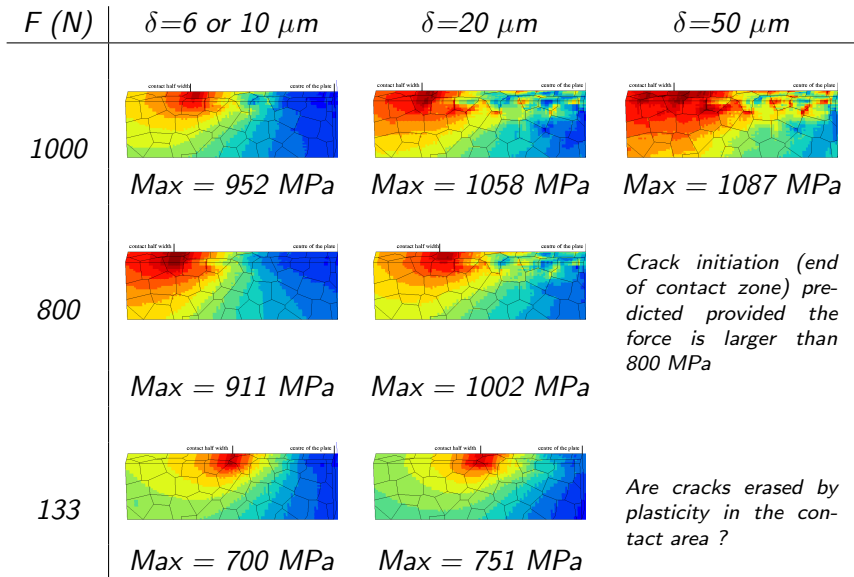
Fretting damage map



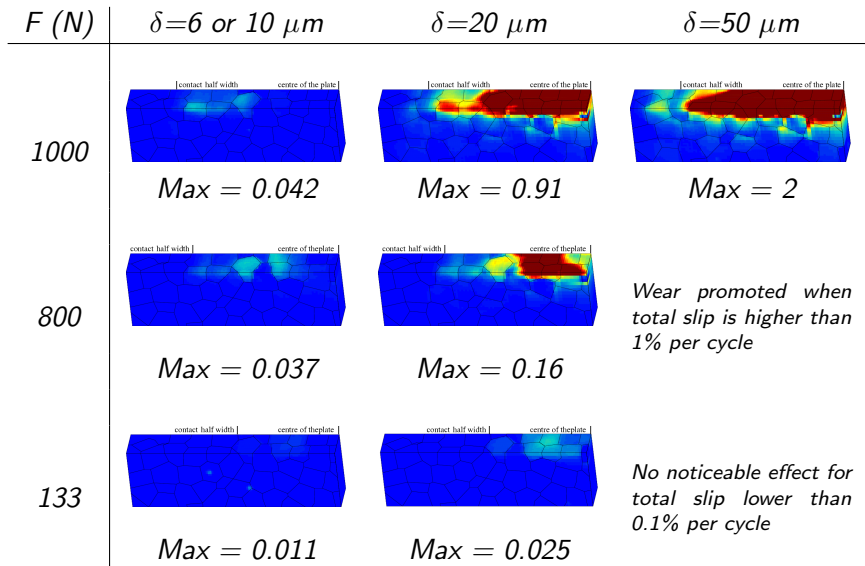
Fretting damage map



Dang Van equivalent stress fields after 20 cycles



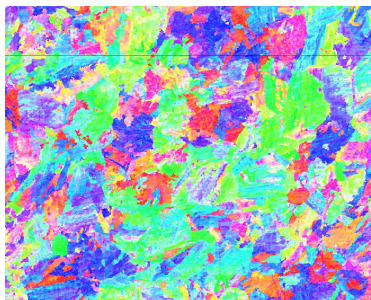
Total slip fields after 20 cycles



Contents

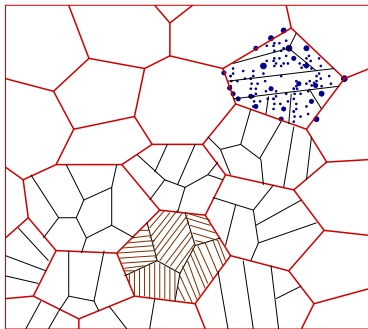
- 1 Macroscopic models
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Microstructure description, 16MND5 bainitic steel



100.0 μm = 100 steps IPF [001]

EBSD image

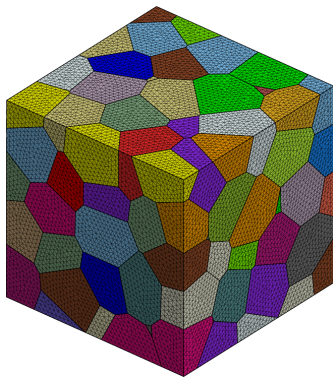


Schematic view

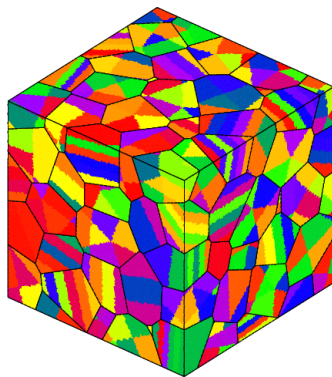
- grain size = $50\mu\text{m}$
- packet size = $15\mu\text{m}$
- lath size = $2\mu\text{m}$
- carbide size = $1\mu\text{m}$

PhD. Nikolay Osipov, dec. 17, 2007

Synthetic microstructure of austenitic and bainitic phases

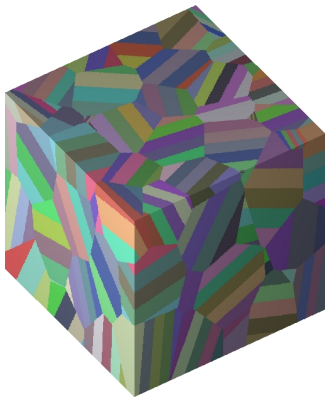


*Austenitic phase represented
by 120 Voronoi grains*



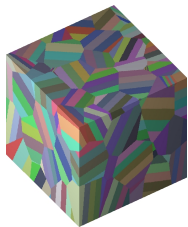
*Bainitic microstructure
≈ 1000 bainitic packets
3 types of cutting*

Steps to generate a free-free mesh

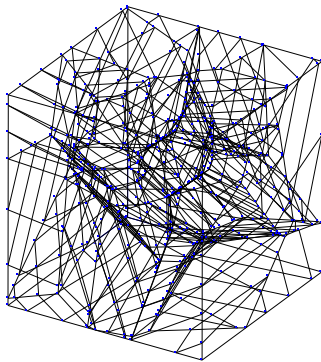


*Image
generation*

Steps to generate a free-free mesh

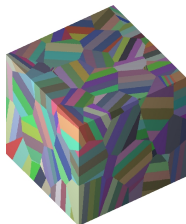


*Image
generation*

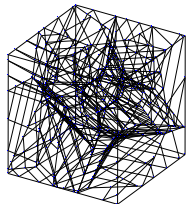


*Geometry
reconstruction*

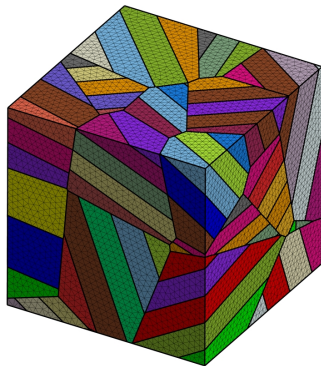
Steps to generate a free-free mesh



*Image
generation*

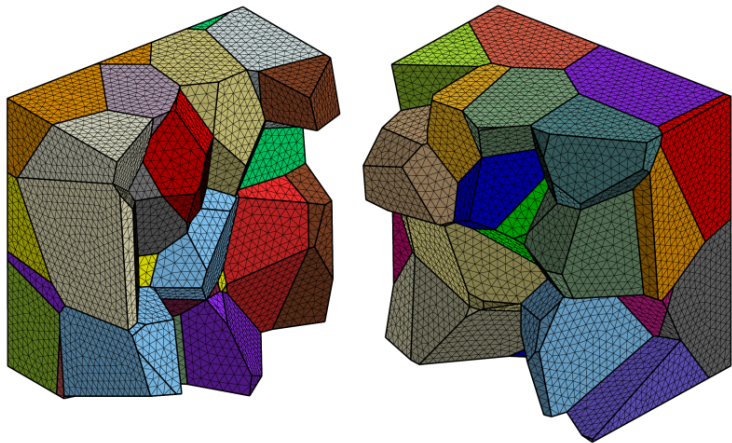


*Geometry
reconstruction*

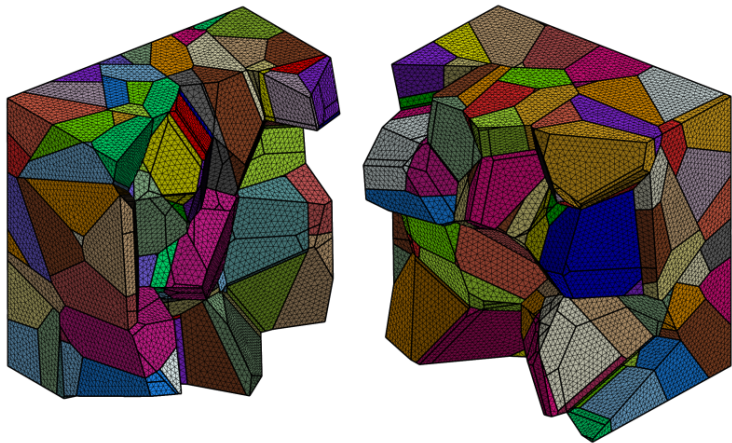


*Free mesh
generation*

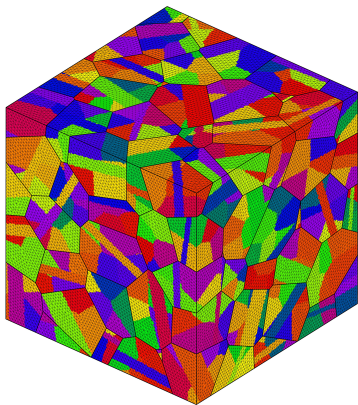
Free mesh of an austenitic microstructure before cutting (50 grains)



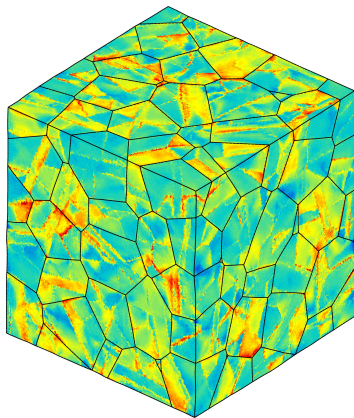
Free mesh of a bainitic microstructure after cutting (50 grains, 245 subgrains)



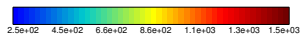
Von Mises stress in the representative volume element



$9 \cdot 10^6$ dof



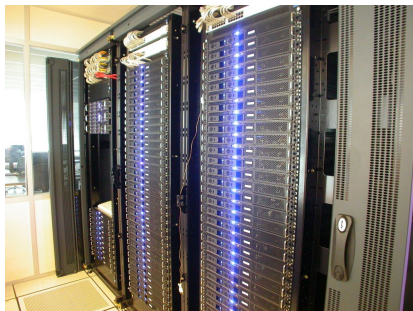
min: 127.58 max: 1770.32



PC clusters



50 processors
32 bits/800 MHz
50 Go memory
2000–2005



224 processors
64bits/2.2GHz
776 Go memory
2005–2009

- *Financial support of Région Ile-de-France and Département de l'Essonne*
- *In connection with Pôle de compétitivité System@tic and Teratec*



Besson, J., Cailletaud, G., Chaboche, J.-L., and Forest, S. (2001).

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*Kanit, T., Forest, S., Galliet, I., Mounoury, V., and Jeulin, D.
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